

## Math Objectives

- Students will explore the validation of a model constructed from a data set.
- Students will be able to determine a regression equation.
- Students will understand that a pattern in the graph of the residuals indicates that the model is not appropriate for the data set.
- Students will look for and express regularity in repeated reasoning (CCSS Mathematical Practice).
- Students will look for and make use of structure (CCSS Mathematical Practice).

## Vocabulary

- data set
- residual
- linear
- exponential




## About the Lesson

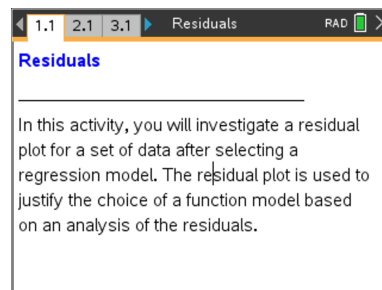
- This lesson includes modeling a data set using linear and exponential regressions.
- As a result students will:
  - Observe a residual plot as well as a scatter plot of the data.
  - Understand that a residual is the actual value of the data minus the predicted value from the regression equation.
  - Conjecture and draw conclusions about the appropriateness of the model based on the residual plot.

## TI-Nspire™ Navigator™

- Send the TI-Nspire document to students.
- Use Class Capture to view and discuss the scatter plots and residual plots.
- Use Quick Poll questions to adjust the pace of the lesson according to student understanding.

## Activity Materials

- Compatible TI Technologies:  TI-Nspire™ CX Handhelds,  TI-Nspire™ Apps for iPad®,  TI-Nspire™ Software



## Tech Tips:

- This activity includes screen captures taken from the TI-Nspire CX handheld. It is also appropriate for use with the TI-Nspire family of products including TI-Nspire software and TI-Nspire App. Slight variations to these directions may be required if using other technologies besides the handheld.
- Watch for additional Tech Tips throughout the activity for the specific technology you are using.
- Access free tutorials at <http://education.ti.com/calculators/pd/US/Online-Learning/Tutorials>

## Lesson Files:

### Student Activity

- Residuals\_Student.pdf
- Residuals\_Student.doc

### TI-Nspire document

- Residuals.tns

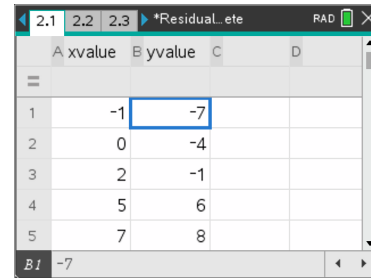
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**Part 1**

Use the following data set in Part 1.

$x$	-1	0	2	5	7	10
$y$	-7	-4	-1	6	8	16

- Enter the  $x$  values in the column labeled  $xvalue$ . Enter the  $y$  values in the column labeled  $yvalue$ .



**Tech Tip:** Students must press enter or the down arrow after the last value is entered.

Add a page by pressing **ctrl** **doc**. Select>Add Calculator. Press **menu**. Select> Statistics> Stat Calculations, then Linear Regression ( $mx + b$ ). For X List: select  $xvalue$  and for Y List: select  $yvalue$ . Press enter for OK..

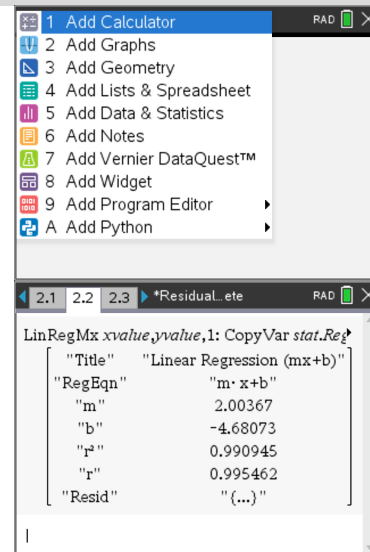
What is your linear regression equation?

**Answer:** The linear regression equation is

$$y = mx + b$$

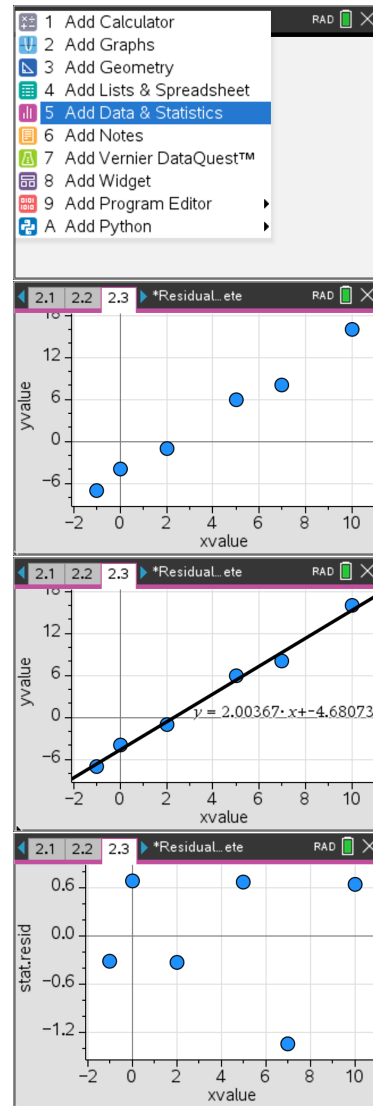
$$m = 2.00367$$

$$b = -4.68073$$



2. Add a page by pressing  $\text{ctrl} \text{ doc} \downarrow$ . Select > Add Data & Statistics. Click in the lower gray region to select xvalue and click in the left gray region to select yvalue.

**Note:** To show the graph of the linear regression equation, press  $\text{menu}$ . Select > Analyze > Regression, and Show Linear (mx + b). To hide the graph of the linear regression equation, press  $\text{menu}$ . Select 4 > Analyze > Regression, and Hide Linear (mx + b).

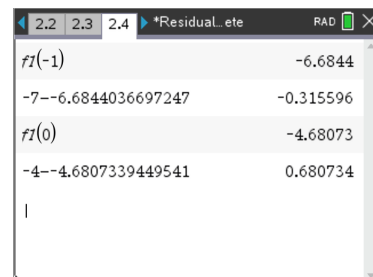


The residual is the actual value minus the predicted value. A regression model is justified as appropriate for a data set if the residuals of a regression, the residual plot, appear without pattern. To view the residual plot, click in the left gray region and select stat.resid.

Does your residual plot have a pattern? Would a linear regression be appropriate for this data set?

**Answer:** The residual plot does not have a pattern. A linear regression is appropriate for this data set.

3. Add a page by pressing  $\text{ctrl} \text{ doc} \downarrow$ . Select > Add Calculator. To evaluate the predicted values, type  $f1(-1)$  and then calculate the residual when x is -1. Calculate  $f1(0)$  and then calculate the residual when x is 0. Notice that one residual value is negative and one is positive. What does this tell us about the predicted value as being an underestimate or an overestimate?



$f1(-1)$	-6.6844
$-7 - -6.6844036697247$	-0.315596
$f1(0)$	-4.68073
$-4 - -4.6807339449541$	0.680734



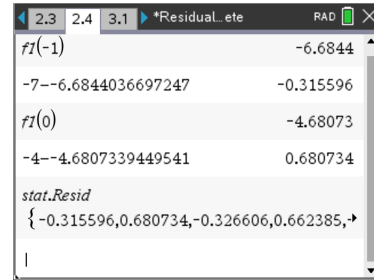
**Answer:**

$f1(-1) = -6.68440367$ ; Residual =  $-0.31559633$

$f1(0) = -4.680733945$ ; Residual =  $0.680733945$

If the residual is positive, the predicted value is an underestimate. If the residual is negative, the predicted value is an overestimate.

**Note:** To view the residual list for all of the data points, press  $\boxed{\text{var}}$  and select stat.Resid. Scroll to the right to see more values.



**Teacher Note:** The graph of the scatter plot with the regression equation may be helpful to visualize the overestimate or underestimate.

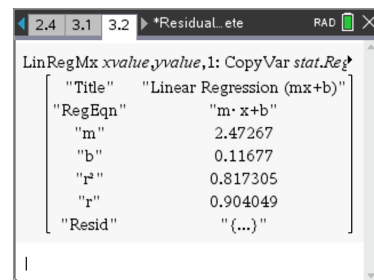
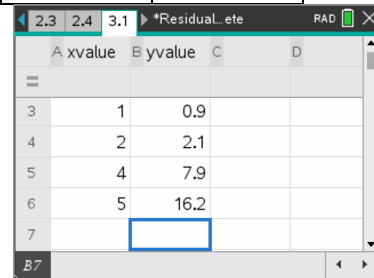
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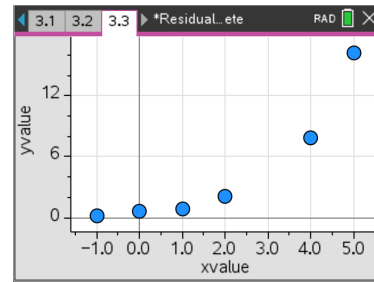
### Part 2

Use the following data set in Part 2.

$x$	-1	0	1	2	4	5
$y$	0.2	0.6	0.9	2.1	7.9	16.2

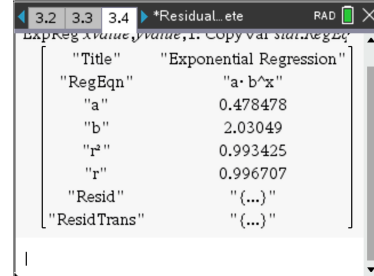
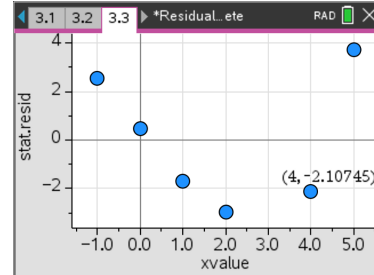
4. Follow the steps in Part 1. Enter the  $x$  values in the column labeled  $xvalue$ . Enter the  $y$  values in the column labeled  $yvalue$ . Compute a linear regression, view the scatter plot, and view the residual plot. Does your residual plot have a pattern? Would a linear regression be appropriate for this data set?



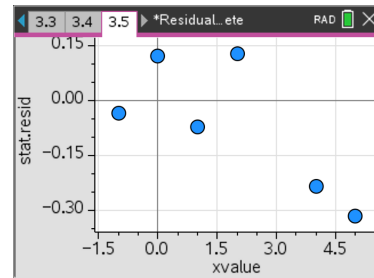


**Answer:** The residual plot appears to have a pattern. A linear regression is not appropriate for this data set.

- Now compute an exponential regression. Add a page by pressing **ctrl** **doc**. Select > Add Calculator. Press **menu** . > Statistics, >Stat Calculations, then \ Exponential Regression. View the residual plot. Does your residual plot have a pattern? Would an exponential regression be appropriate for this data set?



**Answer:** The residual plot does not appear to have a pattern. An exponential regression is appropriate for this data set.



**Extensions**

- Find a data set that models a quadratic and ask the students to follow the steps for a quadratic regression. Observe the scatter plot and the residual plot.

**Wrap Up**

Upon completion of the lesson, the teacher should ensure that students are able to understand:

- How to input data and view scatter plots.
- How to compute linear, quadratic, and exponential regressions.
- How to plot residuals and determine if the residual plot has a pattern.